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Angle between two vectors 3d python

Another short post related to a question I was asked, that I thought might be helpful to others. Getting the angle between two vectors in 2D is as simple as: var angle = Math.atan2(vectorA.y - vectorB.y, vectorA.x - vectorB.x) However, that does not work in 3D space, however the angle between any two vectors (2D or 3D) is defined as cosinus theta = (A point B) / Normalized-A * Normalized-B If theta is the angle between them. To find theta, we can reverse the equation: theta = acos((A point B) / Normalized-A * Normalized-B) I studied the product point from vector analysis in my school. Now that formula, I'll use it to find the angle between three points. We use more dimentantial data would be 1D, 2D, 3D and larger sizes, not only 2D. But I explained it with 2D data points. The point product can be defined algebraically or geometrically. The geometric definition is based on the notions of angle and distance (vector scale). The equivalence of these two definitions is based on a Cartesian coordinate system for the Euclidean space. Geometric definition: geometric obect possessing both a magnitude and a direction. A vector can be imagined as an arrow. Its magnitude is its length, and its direction is the direction in which the arrow is heading. The magnitude of a vector is noted by || a||. The point product of the two Euclidian vectors a and b is defined by, where p is the angle between a and b.Explanation: I want to ask a question about the angle between two vectors. I'm a chemistry student studying the angle of connection between two hydrogen atoms using Python. I remember from my last year of high school that the following angle properties between vectors are observed: $\cos \theta = \frac{a \cdot b}{\|a\| \|b\|}$ and received the following three-dimensional vectors in Cartesian form: [0, 0, 0, 0.102249] (Sulf) [0, 0, 0.968059, -0.817992] (Hydrogen 1) [0, 0, -0.968059, -0.817992] (Hydrogen 2) A chart is provided below. I know the vectors of concern are Hydrogen 1 and Hydrogen 2. I know to take their product point to calculate the $\frac{a \cdot b}{\|a\| \|b\|}$ fraction term. However, I was asked to use the numpy's norm() function, which returns a vector or array shape. From what I seem to do out, a vector norm in this case is apparently the same as the length of the vector for example, the module or $\|a\|$ | vector θ | but I'm not sure if this is correct. What is the norm of a vector serve as a purpose for calculating the angle between two vectors θ and θ_2 ? I posted a VBA function to return the angle between two vectors, in 2D or 3D last year, and just discovered that Python and Numpy are devoid of this function. Because all the suggested code I found in a quick search used: $\cos \theta = (a \cdot b) / (\|a\| \|b\|)$ that gives inaccurate results small angles, I wrote my own, using the same procedure as the VBA version: $\tan \theta = |\langle ab \rangle / \langle ab \rangle|$ Here is the long-lasting code: import numpy as np import numpy.linalg as at @xl_func(numpy_row v1, numpy_row v2: float) def py_ang(v1, v2): Returns the angle in radians between vectors 'v1' and 'v2' $\cos \theta = \frac{\langle ab \rangle}{\|a\| \|b\|}$ sinang = la.norm(np.cross(v1, v2)) return np.arctan2(sinang, cosang) For details about connecting to Python functions in Excel using Pyxll see: Install Python, Scipy, and Pyxll; also updated Glob_to_Loc function, using the py_ang function, will appear in the next few days. Relying on the large sgn_pepper response and the addition of support for aligned vectors, plus adding a speedup of more than 2x using Numba @njit(cache=True, nogil=True) def angle(vector1, vector2): Returns the angle in radians between vectors given v1_u = unit_vector(vector1) v2_u = unit_vector(vector2) minor = np.linalg.det(np.stack(v1_u[2:], v2_u[2:]))) if minor == 0: sign = 1 something else: sign = -np.sign(minor) dot_p = np.dot(v1_u, v2_u) dot_p = min(dot_p, -1.0, 1.0) return sign * np.arccos(dot_p) @njit(cache=True, nogil=True) def unit_vector(vector): Returns the vector vector return vector / np.linalg.norm(vector) def test_angle(): def npf(x): return np.array(x, dtype=float) affirm np.isclose(angle(npf(1, 1)), npf(1, 0))), pi / 4) affirm np.isclose(angle(npf(1, 0)), npf(1, 1))) -pi/4) affirm np.isclose(angle(npf(0, 1)), npf(1, 0), npf(0, 0))) pi/2) affirm np.isclose(angle(npf(1, 0), npf(0, 0))) 0) affirm np.isclose(angle(npf(1, 0), npf(-1, 0))) pi) affirm 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